

14.8. 5, 7.

5.) $\int_1^4 \frac{dx}{x^2}$, Simpson's Rule, $n=4$.

$a=1$
 $b=4$
 $f(x) = \frac{1}{x^2}$

$\int_a^b f(x) dx \approx \frac{h}{3} [f(a) + 4f(a+h) + 2f(a+2h) + \dots + f(b)]$. $h = \frac{4-1}{4} = \frac{3}{4}$.

$\int_1^4 \frac{1}{x^2} dx \approx \frac{3}{4} [f(1) + 4f(1+\frac{3}{4}) + 2f(1+2 \cdot \frac{3}{4}) + 4f(1+3 \cdot \frac{3}{4}) + f(4)]$

$= \frac{1}{4} [f(1) + 4f(\frac{7}{4}) + 2f(\frac{10}{4}) + 4f(\frac{13}{4}) + f(4)]$

$= \frac{1}{4} [\frac{1}{1^2} + 4 \frac{1}{(\frac{7}{4})^2} + 2 \frac{1}{(\frac{10}{4})^2} + 4 \frac{1}{(\frac{13}{4})^2} + \frac{1}{4^2}]$

$= \frac{1}{4} (3.067) = \boxed{0.7668}$

$a=0$
 $b=2$
 $f(x) = \frac{x}{x+1}$
 $h = \frac{2-0}{4} = \frac{1}{2}$

7.) $\int_0^2 \frac{x}{x+1} dx$, Trap. Rule, $n=4$.

$\int_a^b f(x) dx \approx \frac{h}{2} [f(a) + 2f(a+h) + 2f(a+2h) + 2f(a+3h) + \dots + f(b)]$

$\int_0^2 \frac{x}{x+1} dx \approx \frac{1}{2} [f(0) + 2f(0+\frac{1}{2}) + 2f(0+2 \cdot \frac{1}{2}) + 2f(0+3 \cdot \frac{1}{2}) + f(2)]$

$= \frac{1}{4} [f(0) + 2f(\frac{1}{2}) + 2f(1) + 2f(\frac{3}{2}) + f(2)]$

$= \frac{1}{4} [\frac{0}{0+1} + 2 \frac{\frac{1}{2}}{\frac{1}{2}+1} + 2 \frac{1}{1+1} + 2 \frac{\frac{3}{2}}{\frac{3}{2}+1} + \frac{2}{2+1}]$

$= \frac{1}{4} [\frac{1}{\frac{1}{2}+1} + 1 + \frac{3}{\frac{3}{2}+1} + \frac{2}{3}] = \boxed{0.883}$